

# Lecture 11: Radioactive Decay

1. Mechanisms
2. The decay equation

*We acknowledge and respect the lək'əŋən peoples on whose traditional territory the university stands and the Songhees, Esquimalt and W̱SÁNEĆ peoples whose historical relationships with the land continue to this day.*



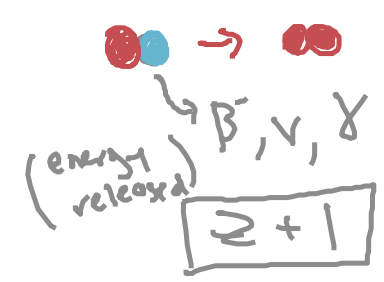
# Mechanisms of radioactive decay.

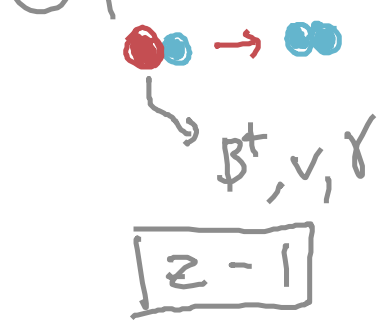
Carbon-12  $C^{12}$   $A = \text{atomic mass}$

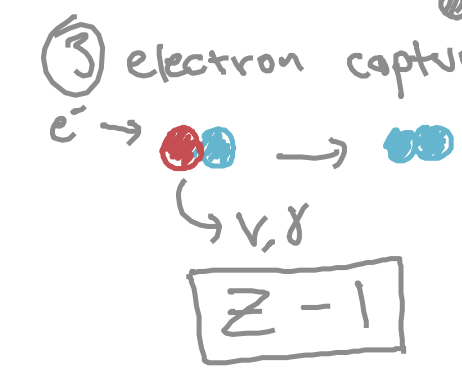
$\beta$  decay: change  $Z$ , no change in  $A$

$\nu = \text{neutrino}$   
 $\gamma = \text{gamma radiation}$

$\bullet = N$   
 $\bullet = P$

① negatron decay  

 $\beta^-, \nu, \gamma$   
 $Z + 1$

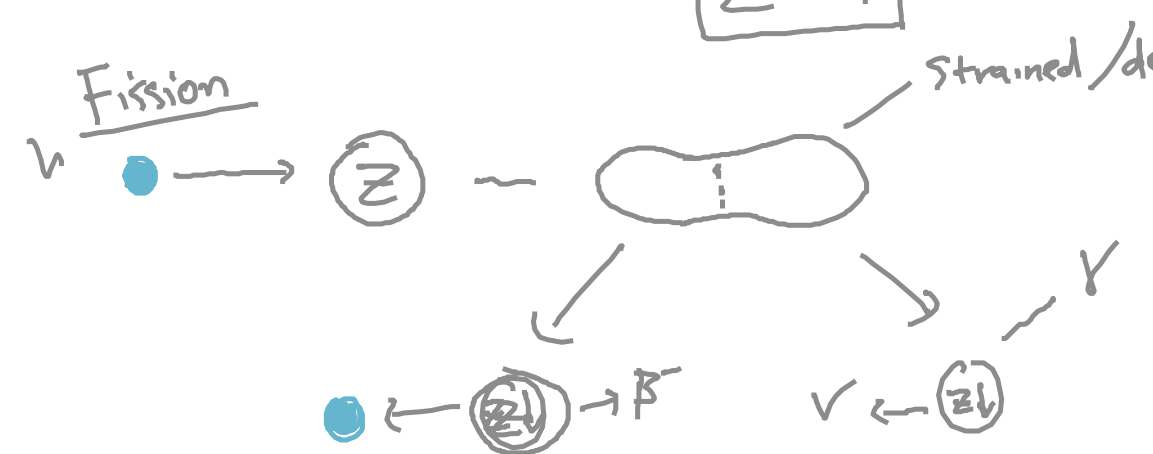
② positron decay  

 $\beta^+, \nu, \gamma$   
 $Z - 1$

③ electron capture  

 $e^- \rightarrow \nu, \gamma$   
 $Z - 1$

isotopes: same # ~~of~~ protons  $Z$  versus different  $N$  neutrons  
 electric force versus nuclear binding energy (nucleus length scale)

$z \text{ H-2} + \text{H-2} \rightarrow \text{He-4}$

Alpha decay  
 $A=238$   
 $Z=92$   $(U)$   $\xrightarrow{\text{high energy}}$   $\alpha$  (alpha particle)  $\rightarrow$   $(Th)$   $A=234$   $Z=90$   
 \* can damage crystal lattices as released

Fission  

 $\nu \rightarrow (Z) \rightarrow \text{strained/deformed} \rightarrow (Z1) \rightarrow \beta^-$   
 $\nu \leftarrow (Z2) \rightarrow \gamma$



# The decay equation.

Rutherford + Soddy 1902

$N$  = number of moles of an isotope

$$\frac{dN}{dt} \propto N$$

$$\frac{dN}{dt} = -\lambda N$$

↖ proportionality constant  
decay constant

$$\int \frac{dN}{N} = \int -\lambda dt$$

$$\ln N - \ln C = -\lambda t$$

$$\ln \frac{N}{C} = -\lambda t$$

$$e^{-\lambda t} = \frac{N}{C}$$

$$C e^{-\lambda t} = N$$

$$N_0 e^{-\lambda t} = N$$

$\ln x \left| \frac{dx}{x} \right.$

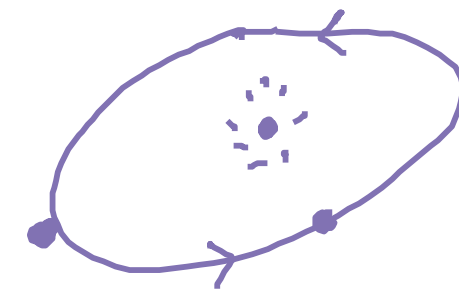
$N_0$  = initial concentration of  $N$

Experiments to test "constant"

↳ high vs low  $T$

↳ high or low  $P$

↳ high vs low magnetic field



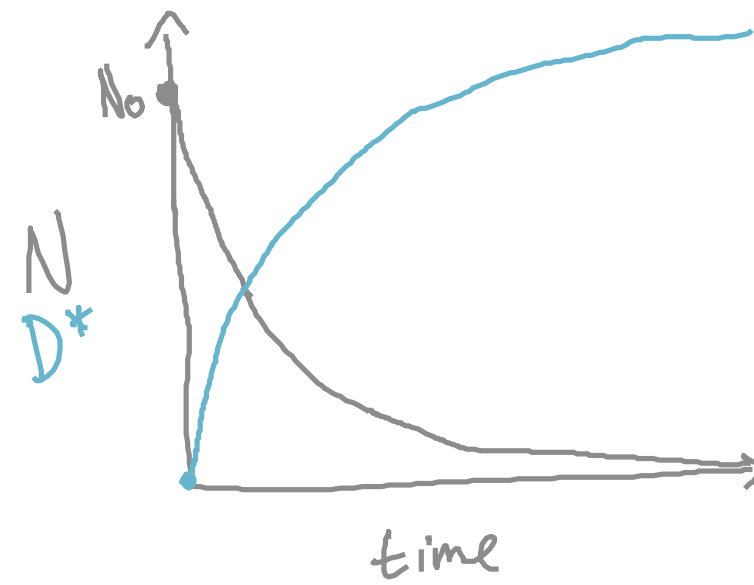
no change from gravity



# The decay equation.

$$N_0 e^{-\lambda t} = N$$

$\uparrow$  not measurable       $\uparrow$  measurable  
 measurable



$N$  = parent isotope

$D$  = descendant isotope

$$N_0 e^{-\lambda t} = N$$

$$N e^{\lambda t} = N_0$$

reversible

$$D^* = N_0 - N$$

Descendant created by the decay of  $N$

$$D^* = N e^{\lambda t} - N_0 e^{-\lambda t}$$

$-\lambda t$  \* hard to measure absolute values, so ratio w/ stable isotope common

$$D^* = N (e^{\lambda t} - 1)$$

$\uparrow$  measured

$$\frac{D}{x} = \frac{D_0}{x} + \frac{N}{x} (e^{\lambda t} - 1)$$

$$D = D_0 + D^*$$

$\uparrow$  initial D       $\uparrow$  generated D



